Abstract—a watermarking scheme for Grayscale image is proposed based on a family of the chaotic maps and discrete cosine transform. Jacobian Elliptic maps employed to encrypt of watermarked logo. Piecewise nonlinear chaotic map is also used to determine the location of DCT coefficients for the watermark embedding. The purpose of this algorithm is to improve the shortcoming of watermarking such as small key space and low security. Therefore the size of key space for initial conditions and control parameters is computed about $2^{125}(10^{128})$ and this key space is large enough to resist the attacks. To evaluate the robustness and effectiveness of proposed method, several attacks are applied to the watermarked image and the best results have been reported.

Keywords-Blind Digital Image Watermarking, Chaos, Discrete Cosine Transform, Multiple Chaotic Maps, Jacobian Elliptic Map, Piecewise nonlinear chaotic Map

I. INTRODUCTION

Watermarking technique can be used for protection of multimedia information, content authentication, and so on [1]. Digital Watermarking techniques can be broadly classified into two categories: Spatial [2] and Transform [3] domain methods. These types of watermark generation schemes require initial value and the function seed to recreate the same watermark at a later stage[4]. One of the advantages of these Watermarking methods is the possibility to analyze and control their spectral properties [5]. In most spatial domain schemes, watermark signal is embedded in the LSB (least significant bit) of the pixels in host image in which the robustness against attacks is weak i.e. watermark can be detected easily [6]. Wavelet transform is widely used for digital watermarking, where one of the most well-known methods is Cox’s watermark embedding scheme [7]. The discrete cosine transform (DCT) is a technique for converting a signal into frequency components which was used first time in 1974 [8]. It is widely used in image compression[9]. The DCT has special property that most of the visually significant information of the image is concentrated in just a few coefficients of the DCT. It’s referred as ‘Energy compaction Property’ [10]. The DCT coefficients can be quantized using visually-weighted quantization values.

Two main requirements for an acceptable watermarking technique are imperceptibility[11] and robustness[12]. Imperceptibility refers to perceptual quality of the data being protected. Robust watermarking embeds information data within the image with an insensible form for human visual system, but in a way that protects from attacks such as common image processing operations.

In authentication watermarking, tamper localization and detection accuracy are two issues performances. However, most of presented methods in the studied literature cannot obtain precise localization. A watermark typically contains information about origin, status, and/or destination of the host data [13], [14]. Image scrambling is one of the most prevailing encryption algorithms these years [15], [16], [17]. However, these methods are not so many. The majority of watermarking schemes proposed to date, use watermarks generated from pseudo random number sequences [18].

The first Chaotic system has been discovered by Edward Lorenz in 1963[19]. Other chaotic systems have been established by many different research areas, such as physics, mathematics, and engineering. The idea of using chaotic signals in different layers of communication systems attracted the attention of researchers [20-25].

This paper chiefly focuses on the application of piecewise nonlinear chaotic map [26] and jacobian elliptic [27] in encryption techniques of watermark logo. Piecewise nonlinear chaos and jacobian elliptic chaos began as an attempt to find chaos in the sense of extreme sensitivity to changes in initial conditions. Chaotic functions such as Markov Maps, Bernoulli Maps, Skew Tent Map, and Logistic Map have been widely used to generate watermark sequences [28], [29].

In our previous work, we used the chaos coupled maps and DWT for blind digital watermarking [30]. In that paper the chaotic maps are employed to improve the security of a watermarked image, and an improved mutation operator has been used to encrypt the watermark logo. The upgraded mapping method determines the location of DWT coefficients where the watermark is embedded.

In this paper multiple chaotic maps are employed to enhance security and the best extraction, and these maps are also used to determine the location of DCT coefficients for the watermark embedding. We also use XOR operator to encrypt the watermark logo.

This paper is organized as; section II describes chaotic maps for scrambling process, and section III presents a Discrete Cosine Transform. The details of watermark embedding and extraction are presented in section IV. Some simulation results
are discussed in Section V and the paper is concluded in Section IV.

II. APPLIED CHAOTIC MAPS

A. Jacobian Elliptic Maps

One-parameter families of jacobian elliptic rational maps[31] of the interval \([0,1]\) with an invariant measure can be defined as:

\[
X_{n+1} = \frac{4a^2x^2_x X_n(1-x_N)}{(1-k^2 x^2_n + 4(a^2-1)x_n(1-x_N))} \quad (1)
\]

Where \(X_0 \in [0,1], \alpha \in [0,4], k \in [0,1] \) (modulus) represents the parameter of the elliptic functions. The 3D bifurcation behavior of System is shown in Fig.1 (a). Fig.2 (a) shows the pseudo-random generation in 5000 iterations by Eq.(1) and histogram of the pseudo-random values is shown in Fig.2 (b).

Jacobian elliptic map is used in this paper as follow:

\[
C_{X_{n+1}^1} = \begin{cases} 0 & X_{n+1} \leq 0.5 \\ 1 & X_{n+1} > 0 \end{cases} \quad (2)
\]

B. Piecewise nonlinear chaotic Map

We present a brief review of one-parameter families of piecewise nonlinear chaotic maps with an invariant measure. These maps can be defined as:

\[
X_{n+1} = \frac{\alpha^2 F}{1+(\alpha^2-1) F} \quad (3)
\]

Where

\[
F = \begin{cases} \frac{X_n}{P} & 0 \leq X \leq P \\ \frac{X_n-P}{1-P} & P < X \leq 1 \end{cases} \quad (4)
\]

Then, the probability parameter of the piecewise nonlinear chaotic maps \(p\) is generated by using the results of iteration of the trigonometric map can be defined as:

\[
Y_{n+1} = \frac{1}{\beta^2} \tan^2(N \times \arctan(\sqrt{X_n})) \quad (5)
\]

Therefore

\[
P = \begin{cases} \frac{Y_{n+1}}{Y_{n+1}} & 0 \leq Y_{n+1} \leq 1 \\ \frac{1}{Y_{n+1}} & Y_{n+1} > 1 \end{cases} \quad (6)
\]

Where \(X_0 \in [0,1], \alpha \in [0,4], \beta \in [0,4], Y_0 \in [0,1], b \in [1,4] \) and \(P \in [0,4]\).

The 3D bifurcation behavior of System is shown in Fig.1 (b). Fig.2 (c) shows the pseudo-random generation in 5000 iterations by Eq. (3) and histogram of the pseudo-random values is shown in Fig.2 (d).

This map is used for embedding and extraction process as follow:

\[
\begin{cases}
CX_{n+1}^1 = (X_{n+1} \times 10^{14}) \mod M \\
CY_{n+1}^2 = (Y_{n+1} \times 10^{14}) \mod N
\end{cases} \quad (7)
\]

C. Elliptic map for watermark logo encryption

The watermark logo encryption proposed in this paper consists of the following major steps:

- The plain logo \(W_{\text{m} \times n}\) is transformed into a one-dimensional array \(W_{\text{m} \times \text{m} \times 1}\).
- The secret keys, including initial conditions and control parameters are set, and chaotic map in Eq.(2) are iterated 500 times.
- Ciphered values is computed by:
  \[
  C_i = (CX^1_{i \times 1} \text{ XOR } W_i)
  \]
  (Where \(C_i\) is one dimensional array considered for storing the ciphered value).
- When all the pixels were encrypted, the matrix \(C_{\text{m} \times \text{n} \times 1}\) is transformed into \(C_{\text{m} \times \text{n}}\) and cipher watermark logo is exported to next step of watermarking algorithm.
- Process of decryption is very similar to the encryption process. Just steps mentioned in the encryption process are repeated.

![Fig.1. Bifurcation of (a) Jacobian elliptic Map (b) Piecewise nonlinear chaotic Map.](http://journals.usb.ac.ir/IJCIT/en-us/MainPage)
D. Selecting Location embedded by Piecewise nonlinear chaotic Map

Using the coordinate \((i,j)\) position of watermark pixel as the initial condition and through setting a value for the control parameter in Eq.(7), chaotic map is iterated after which, the embedding position of the pixels from the watermark image to host image can be obtained. The watermark pixels will get different embedding positions, so, the embedded watermark pixels will spread on the host image randomly.

I. DISCRETE COSINE TRANSFORM

Define the orthogonal matrix \(U\) of order \(m\) by

\[
U(i,j) = \begin{cases} 
\frac{1}{\sqrt{m}} & i = 1 \\
\sqrt{\frac{2}{m}} \cos\left(\frac{n(2j-1)(i-1)}{2m}\right) & 2 \leq i \leq m 
\end{cases} \tag{8}
\]

The orthogonal matrix \(V\) of order \(n\) is defined similarly with \(m\) replacing \(n\) in (8). The discrete cosine transform (DCT) of an image matrix \(A\) is defined by

\[
X = UAV^T \tag{9}
\]

And the inverse discrete cosine transform (IDCT) of \(X\) is defined by

\[
A = U^TXXV \tag{10}
\]

In the proposed method, Watermark Logo is inserted in the middle coefficients. Fig. 3 shows the insertion area.

II. WATERMARK EMBEDDING AND EXTRACTION

Block diagram of proposed embedding and extraction process are shown in Fig.(4).

A. Watermark embedding

The embedding process proposed in this paper consists of the following major parts:

- Encryption process is applied to input watermark logo.
- Original image using 2D discrete Cosine transform are decomposed into coefficients as Fig. 3.
- In this step, embedding location of watermark logo is obtained by Eq. (2).

- Figure 2. (a) The pseudo-random generation in 5000 iterations by Eq. (1) (b) Histogram of the pseudo-random values for 5000 iterations by Eq. (1) (c) The pseudo-random generation in 5000 iterations by Eq. (3) (d) Histogram of the pseudo-random values for 5000 iterations by Eq. (3)

- Fig.2. Embedding location in DCT coefficients

- Fig.3. Block Diagram of (a) embedding process (b) extraction process
Neighborhoods of central coefficient are determined (See Fig.5). In this paper, neighborhood type in Fig.5 (a) is used in embedding and extraction process.

- Calculate Minimum and maximum of coefficients in Fig.5. (a) and store in MAX, MIN variables.
- If pixel value of watermark logo equal to 1, central coefficient is replaced by \( MAX + t \), else pixel value of watermark logo equal to 0, central coefficient is replaced by \( MIN - t \) (t is threshold value).
- When all pixels were embedded into coefficients, 2D inverse discrete cosine transform is applied and final watermarked image is obtained.

Flowchart of embedding process is shown in Fig.6.

**B. Watermark extraction**

Watermark extraction process which is very similar to the embedding process consists of the following major parts:

- Watermarked image using 2D discrete cosine transform are decomposed into DCT coefficients.
- Extraction location of watermark logo is obtained by Eq. (5).
- Neighborhoods of central coefficient is determined (See Fig.5. (a)).
- Calculate median of coefficients in Fig.5. (a) and store in Med variable.
- If central coefficient is greater than Med, watermark pixel value is 1, else watermark pixel value is 0;
- When all pixels were extracted from coefficients, Watermark logo decryption is applied and final watermark logo is obtained.

Flowchart of extraction process is shown in Fig.7.

---

**I. EXPERIMENTAL RESULTS**

This section will present and discuss the experimental results of our proposed scheme. Digital watermarking techniques must satisfy the following properties.

---

**Evaluation of the effectiveness**

To demonstrate the effectiveness of the proposed algorithm, MATLAB simulations are performed by using 512x512 pixel gray level “LENA" image and 64 x64 pixel binary watermark logo “USB". Fig. 5 demonstrates the invisibility of watermark. Figs. 8(a-b) show the original host image and watermark logo, respectively. Figs. 8 (c-e) show the watermarked image, the extracted watermark logo by correct keys and the extracted watermark logo by incorrect keys, respectively. The watermark embedding process is said to be imperceptible if the original data and watermarked data cannot be distinguished.
To quantitatively evaluate the performance of the proposed scheme, the peak signal-to-noise ratio (PSNR) was adopted to measure the image quality of a watermarked image which is given by:

$$\text{PSNR} = 10 \times \log_{10} \left( \frac{255^2}{\text{MSE}} \right) \text{ (dB)} \quad (11)$$

According to the definitions in statistics, the mean squared error (MSE) between the original and watermarked images is defined by

$$\text{MSE} = \frac{1}{M \times N} \sum_{i=1}^{M} \sum_{j=1}^{N} (h_{ij} - \hat{h}_{ij})^2 \quad (12)$$

Where $h_{ij}$ and $\hat{h}_{ij}$ indicate the pixel values in the location $(i, j)$ of the original host image and the watermarked image, respectively, while $M \times N$ is the image size. In this study, reliability was measured as the bit error rate (BER) of extracted watermark through this formula:

$$\text{BER} = \frac{B}{M \times N} \times 100 \quad (13)$$

Where, $B$ is the number of erroneously detected bits, and $MN$ is the extracted watermark image dimensions. The PSNR for the watermarked image is 40.51 dB, and the BER of the extracted watermark is zero. Therefore, there is no obvious perceptual distortion between watermarked image and original one; the embedded watermark does not degrade the quality of original host image.

**B. Robustness to attacks**

To test the robustness of our proposed method, we applied several attacks to the watermarked image. In the experiments, both geometric and non-geometric attacks are considered. Non-geometric attacks include:

- JPEG compression: JPEG is the first international image compression standard for continuous-tone still images both grayscale and color images [32], [33].
- Median filtering: In median filtering the input pixel is replaced by the median of the pixels contained in the neighborhood [34].
Fig. 8. Watermarked Image under different attacks:
(a) JPEG compression, (b) Salt & pepper noise 10\%, (c) Gaussian noise \([0,0.01]\) (d) Histogram Equalization, (e) Median filter \([3\times3]\), (f) low-pass filter \([5\times5]\), (g) Gamma correction 0.6 (h) motion blur 45°, (i) Rotation (1°), (j) Cropping (25\%).

Fig. 9. Extracted watermark logo under different attacks:
(a) JPEG compression, (b) Salt & pepper noise 10\%, (c) Gaussian noise \([0,0.01]\) (d) Histogram Equalization, (e) Median filter \([3\times3]\), (f) low-pass filter \([5\times5]\), (g) Gamma correction 0.6 (h) motion blur 45°, (i) Rotation (2°), (j) Cropping (25\%).

- Low-pass filtering: Low-pass filtering attenuates the high frequency components in the signal and is essentially equivalent to integrating the signal. Low-pass filtering of an image is a spatial averaging operation. It produces an output image, which is a smooth version of the original image, devoid of the high spatial frequency components that may be present in the image [35].
- Gamma correction: Gamma correction, gamma nonlinearity, gamma encoding, or often simply gamma, is the name of a nonlinear operation used to code and decode luminance or tristimulus values in video or still image systems.
- Blurring: Blurring is used in preprocessing steps, such as removal of small details from an image prior to (large) object extraction, and bridging of small gaps in lines or curves. Noise reduction can be accomplished by blurring with a linear filter and also by nonlinear filtering [35].
- Sharpening: The principal objective of sharpening is to highlight fine detail in an image or to enhance detail that has been blurred, either in error or as a natural effect of a particular method of image acquisition.
- Histogram equalization: Histogram equalization is a technique which consists of adjusting the gray scale of the image so that the gray level histogram of the input image is mapped onto a uniform histogram [35], [36], [37].

And the geometric attacks include:
- Rotation: Rotation of an input image about an arbitrary pivot point can be accomplished by translating the origin of the image to the pivot point, performing the rotation, and then translating back by the first translation offset [35].
- Gaussian noise: Gaussian noise is a statistical noise that has a probability density function of the normal distribution. In other words, the values that the noise can take are Gaussian-distributed. It is most commonly used as additive white noise to yield additive white Gaussian noise [35], [36], [37].
- Salt & Pepper noise: Salt and pepper noise is a form of noise typically seen on images. It represents itself as randomly occurring white and black pixels [35], [36], [37].
- Cropping: Cropping refers to the removal of the outer parts of an image to improve framing, accentuate subject matter or change aspect ratio [38], [39], [40].

Fig. 9 shows an example of a watermarked image, LENA, which is attacked by the listed attacks. The corresponding best extracted watermarks are shown in Fig. 10. The test results for “LENA” image are shown in Table 1 and Table 2.

C. Key Space
The key is the fundamental aspect of every cryptosystem. An algorithm is as secure as its key. No matter how strong and well designed the algorithm might be, if the key is poorly chosen or the key space is small enough, the cryptosystem will be broken. The size of the key space is the number of
encryption/decryption key pairs that are available in the cipher system.

In the proposed scheme, the secret key includes nineteen control and initial conditions parameter of the four chaotic maps. The sensitivity to these initial parameters is shown as follows:

- **JacobianElliptic Map:** $X_0 \in [0,1], \alpha \in [0,4], k \in [0,1].$
- **Piecewise Nonlinear Chaotic Map:** $X_0 \in [0,1], \alpha \in [0,4], \beta \in [0,4], Y_0 \in [0,1], b \in [1,4] \text{ and } P \in [0,4].$

If the precision is $10^{-16}$ for each of 8 parameters, the size of key space for initial conditions and control parameters is $2^{425}((10^{16})^8 = 10^{128}$). The key space is large enough to resist all kinds of brute-force attacks [41].

---

**Table 1**

<table>
<thead>
<tr>
<th>Attack</th>
<th>Lena</th>
<th>Pepper</th>
<th>Barbara</th>
</tr>
</thead>
<tbody>
<tr>
<td>Without Attacks</td>
<td>40.21</td>
<td>43.29</td>
<td>36.18</td>
</tr>
<tr>
<td>JPEG compression (75%)</td>
<td>37.63</td>
<td>38.03</td>
<td>34.58</td>
</tr>
<tr>
<td>Salt &amp; Pepper noise 10%</td>
<td>27.61</td>
<td>41.88</td>
<td>35.87</td>
</tr>
<tr>
<td>Gaussian noise (0,0.01)</td>
<td>31.42</td>
<td>31.50</td>
<td>31.35</td>
</tr>
<tr>
<td>Histogram Equalization</td>
<td>27.87</td>
<td>29.71</td>
<td>30.63</td>
</tr>
<tr>
<td>Median Filtering [3x3]</td>
<td>37.99</td>
<td>38.56</td>
<td>33.41</td>
</tr>
<tr>
<td>Low pass filter</td>
<td>40.15</td>
<td>41.18</td>
<td>34.87</td>
</tr>
<tr>
<td>Gamma Correction 0.6</td>
<td>27.61</td>
<td>27.22</td>
<td>26.93</td>
</tr>
<tr>
<td>Motion Blur 15°</td>
<td>32.49</td>
<td>32.65</td>
<td>30.76</td>
</tr>
<tr>
<td>Rotation 1°</td>
<td>31.98</td>
<td>32.14</td>
<td>30.06</td>
</tr>
<tr>
<td>Cropping (25%)</td>
<td>27.51</td>
<td>27.65</td>
<td>27.30</td>
</tr>
<tr>
<td>Sharpening</td>
<td>39.43</td>
<td>29.83</td>
<td>28.76</td>
</tr>
<tr>
<td>Complement</td>
<td>27.43</td>
<td>27.50</td>
<td>27.94</td>
</tr>
</tbody>
</table>

---

**Table 2**

---

![Fig.10. (a) Original Barbara image (b) watermarked Barbara (c) histogram of original image (d) histogram of watermarked image. Extracted watermarks under different attacks include: (e) JPEG compression (f) Salt & pepper noise 10% (g) Gaussian noise [0,0.01] (h) Histogram Equalization (i) Median filter [3x3] (j) low-pass filter [5x5] (k)Gamma correction 0.6 (l) motion blur 45° (m) Rotation (1°) (n) Cropping (25%) (o) Sharpening (p) complement.](http://journals.usb.ac.ir/IJCIT/en-us/MainPage)
SIMULATION RESULTS OF BER UNDER DIFFERENT ATTACKS

<table>
<thead>
<tr>
<th>Attack</th>
<th>Lena</th>
<th>Peppers</th>
<th>Barb ara</th>
</tr>
</thead>
<tbody>
<tr>
<td>Statistical Test</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Elliptic jacobian</td>
<td>0.4067</td>
<td>0.1901</td>
<td>succes</td>
</tr>
<tr>
<td>p-value (m=128)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Block Frequency</td>
<td>0.4900</td>
<td>0.1827</td>
<td>succes</td>
</tr>
<tr>
<td>(m=128)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Cusum-Forward</td>
<td>0.6577</td>
<td>0.1252</td>
<td>succes</td>
</tr>
<tr>
<td>Cusum-Reverse</td>
<td>0.2771</td>
<td>0.2412</td>
<td>succes</td>
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<tr>
<td>Runs</td>
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<td>0.9551</td>
<td>succes</td>
</tr>
<tr>
<td>Long Runs of Ones</td>
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<td>0.5069</td>
<td>succes</td>
</tr>
<tr>
<td>Rank</td>
<td>0.6861</td>
<td>0.4391</td>
<td>succes</td>
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<tr>
<td>Spectral DFT</td>
<td>0.5146</td>
<td>0.7242</td>
<td>succes</td>
</tr>
<tr>
<td>Non-overlapping Templates (m=9, B=0.000000001)</td>
<td>0.5542</td>
<td>0.2271</td>
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<tr>
<td>Overlapping Template (m=9)</td>
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<td>0.9092</td>
<td>succes</td>
</tr>
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<td>Universal</td>
<td>0.0445</td>
<td>0.4420</td>
<td>succes</td>
</tr>
<tr>
<td>Approximate Entropy (m=10)</td>
<td>0.4419</td>
<td>0.0468</td>
<td>succes</td>
</tr>
<tr>
<td>Random excursions (x=+1)</td>
<td>0.8814</td>
<td>0.3551</td>
<td>succes</td>
</tr>
<tr>
<td>Random excursions Variant (x=-1)</td>
<td>0.5356</td>
<td>0.4264</td>
<td>succes</td>
</tr>
<tr>
<td>Linear Complexity (M=500)</td>
<td>0.8302</td>
<td>0.0395</td>
<td>succes</td>
</tr>
<tr>
<td>Serial (m=16, ( V_{16}^2 ))</td>
<td>0.3680</td>
<td>0.2009</td>
<td>succes</td>
</tr>
<tr>
<td>Without Attacks</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>JPEG compression (75%)</td>
<td>1.92</td>
<td>3.36</td>
<td>1.14</td>
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<tr>
<td>Salt &amp; Pepper noise 10%</td>
<td>14.96</td>
<td>18.60</td>
<td>10.52</td>
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<td>Gaussian noise (0.0.1)</td>
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<td>20.92</td>
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<tr>
<td>Low pass filter</td>
<td>0.24</td>
<td>0.12</td>
<td>0.43</td>
</tr>
</tbody>
</table>

D. The study of the performance of the new algorithm

To evaluate the performance of the new algorithms the PSNR and BER has been computed and compared with some famous benchmarks. Figs. (11-12) show the implementation of the new algorithm on Peppers and Barbara, respectively. The histogram and the extracted logos using different attacks also are presented in these figures. Additionally Table 1 and Table 2 show the comparison of PSNR and BER for the benchmarks. The results conclude of this new watermarking scheme improves the quality of the watermarking as well as increasing the security of images.

E. A Statistical test suit for pesudo random generation for cryptography

The need for random and pseudorandom numbers arises in many cryptographic applications. For example, common cryptosystems employ keys that must be generated in a random fashion. Many cryptographic protocols also require random or pseudorandom inputs at various points. In this paper, we have applied the NIST (National Institute of Standards and Technology) statistical test suites to investigate the randomness of cryptographic random generator numbers. These statistical tests are listed in Table 3. The P-value shows the probability of the randomness of the statistical test suite. If the P-value is very close to one the generated random number passes the test. Therefore the randomness of the generated sequences is accepted. P-value in the range of [0.001,0.01] shows a failure test.

<table>
<thead>
<tr>
<th>Table 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Result of Statistical test suites for pseudo random generators in applied chaotic maps</td>
</tr>
</tbody>
</table>

II. CONCLUDING REMARKS

A new watermarking scheme for blind digital image watermarking based on multiple chaotic maps and DCT transform was proposed. Chaotic Quantum map and Jacobian elliptic map were applied to design the selection scheme for watermark embedding. We have used multiple chaotic maps to increase both the number of keys (control parameters) and complexities involved in the algorithm. The size of key space for initial conditions and control parameters were computed about 10^{128} (2^{425}), Therefore the resistance of the method is the highest in comparison with our previous work.
Furthermore, in this work the maximum amount of data to be stored was 128×128. Finally, according applied multiple chaotic maps, the extracted watermark logo results were much better than our previous work.

REFERENCES


